

## Lecture five

### Topics that must be covered in this lecture:

- Methods of Heuristic search (A\*- algorithm).
  - A\* Algorithm Properties
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### 4- A-Star search algorithm

Minimizing the total estimated solution cost. (A star search).  
 A\* algorithm is simply defined as a best-first search plus a specific function. It evaluates nodes by combining  $g^*(n)$ , the cost to reach the node, and  $h^*(n)$ , the cost to get from the node to the goal:

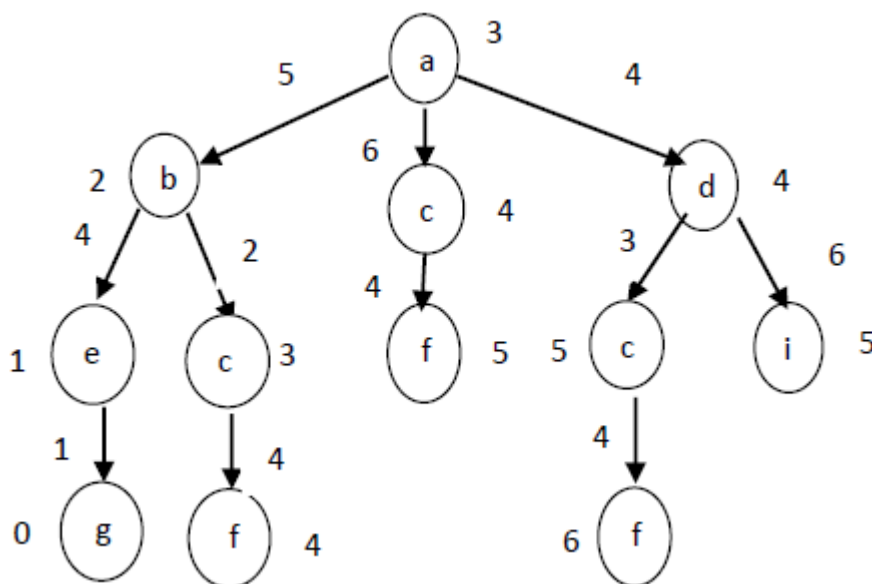
$$F^*(n) = g^*(n) + h^*(n).$$

$g^*(n)$ : The cost to reach the node.

$h^*(n)$ : The cost of node

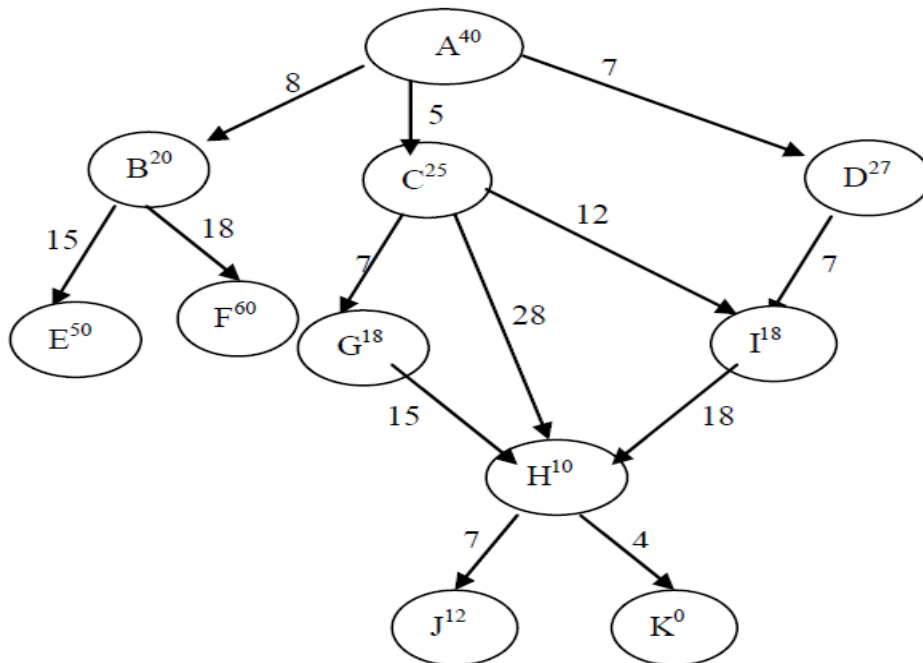
$f^*(n)$ : Value of Heuristic

Function Example:



open	closed
[A3]	[]
[B7,D8,C10]	[A3]
[D8,E10,C10]	[B7,A3]
[E10,C10,115]	[D8,B7,A3]
[G10,C10,115]	[E10,D8,B7,A3]
	[G10,E10,D8,B7,A3]

**Example:** Use A\* algorithm to find the path between A and K for the following search space. Start=[A], goal=K.



open	closed
[A40]	[ ]
[B28,C30,D34]	[A40]
[C30,D34,E73,F86]	[B28, A40]
[G30,D34,I35,H43,E73,F86]	[C30,B28, A40]
[D34,I35,H37,E73,F86]	[G30,C30,B28, A40]
[I32,H37,E73,F86]	[D34,G30,C30,B28, A40]
[H37,E73,F86]	[I32,D34,G30,C30,B28, A40]
[K31,J46]	[H37,I32,D34,G30,C30,B28, A40]

Since K is a goal, stop.

### Properties of Heuristic Function

- 1. Admissibility:** A heuristic function is admissible if it finds the shortest path to a goal state. Note: All A\* algorithms are admissible.
- 2. Monotonicity:** A heuristic function is monotonic if the first visit to any intermediate node gives the shortest path to that node. Note: Each Monotonicity Function is Admissible but not the complement because it chooses the shortest path.
- 3. Informed ness:** A heuristic function  $h_1$  is said to be more informed than a heuristic function  $h_2$  If  $h_1(n) \geq h_2(n)$  for all nodes  $n$ . If  $h_1$  is more informed than  $h_2$  then the subsequence searched by  $h_1$  will be less than that searched by  $h_2$ .